Logistic

Parametrisation

The logistic distribution is

$$f(y) = \frac{\kappa \exp(-\kappa(y - \mu))}{(1 + \exp(-\kappa(y - \mu)))^2}$$

for continuously responses y where

μ: is the the mean

$\kappa = \tau s \pi / \sqrt{3}$: where τ is the precision

s: is a fixed scaling, $s > 0$.

Link-function

The mean and variance of y are given as

$$\mu \quad \text{and} \quad \sigma^2 = \frac{1}{s\tau}$$

and the mean is linked to the linear predictor by

$$\mu = \eta$$

Hyperparameters

The precision is represented as

$$\theta = \log \tau$$

and the prior is defined on θ.

Specification

- family $=$ `logistic`

- Required arguments: y and s (keyword `scale`)

The scalings have default value 1.

Hyperparameter spesification and default values

doc The Logistic likelihoood

hyper

> **theta**
>
>> **hyperid** 72001
>> **name** log precision
>> **short.name** prec
>> **initial** 1
>> **fixed** FALSE
>> **prior** loggamma
>> **param** 1 5e-05
>> **to.theta** function(x) log(x)

from.theta `function(x) exp(x)`

survival FALSE

discrete FALSE

link default identity

pdf logistic

Example

```
rlogistic = function(n, mean = 0, sd = 1)
{
    p = runif(n)
    A = pi/sqrt(3)
    tauA = A/sd^2
    return ((tauA * mean - log((1-p)/p))/tauA)
}

n = 1000
z = rnorm(n, sd=0.1)
eta = 1 + z
y = rlogistic(n, mean = eta,  sd = 1)

r = inla(y ~ 1 + z,  data = data.frame(y, z), family = "logistic",
         control.compute = list(cpo=TRUE))
```

Notes

None.