

Zero-inflated models: Beta-Binomial

Parameterisation

There is support for a further zero-inflated model of type 2 (see zero-inflated.pdf), the zero-inflated beta-binomial. It is only defined for type 2.

Type 2

The likelihood is defined as

$$\text{Prob}(y \mid \dots) = p \times 1_{[y=0]} + (1 - p) \times \text{Beta-binomial}(y)$$

where:

$$p = 1 - \left(\frac{\exp(x)}{1 + \exp(x)} \right)^\alpha$$

Link-function

As for the Binomial (see Zero-inflated.pdf).

Hyperparameters

The Beta-binomial distribution has two arguments (β_1 & β_2) which we assume are a (specific) function of an underlying hyperparameter (δ) & x . There is a further hyperparameter, α , governing zero-inflation where:

The parameter controlling the degree of overdispersion, δ , is represented as

$$\theta_1 = \log(\delta)$$

and the prior is defined on θ_1 .

The zero-inflation parameter α , is represented as

$$\theta_2 = \log(\alpha)$$

and the prior and initial value is is given for θ_2 .

Specification

- `family="zeroinflatedbetabinomial2"`
- Required arguments: As for the zero-inflated-nbinomial2 likelihood.

Hyperparameter spesification and default values

doc Zero inflated Beta-Binomial, type 2

hyper

theta1

hyperid 94001

name log alpha

short.name a

```

    initial 0.693147180559945
    fixed FALSE
    prior gaussian
    param 0.693147180559945 1
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
  theta2
    hyperid 94002
    name beta
    short.name b
    initial 0
    fixed FALSE
    prior gaussian
    param 0 1
    to.theta function(x) log(x)
    from.theta function(x) exp(x)

survival FALSE

discrete FALSE

link default logit loga cauchit probit cloglog ccloglog loglog robit sn

pdf zeroinflated

```

Example

In the following we estimate the parameters in a simulated example.

Example-zero-inflated-beta-binomial2.R

```

nx = 1000                # number of x's to consider
n.trial = 20             # size of each binomial trial
x = rnorm(nx)            # generating x

delta = 10               #hyperparameter 1
p = exp(1+x)/(1+exp(1+x)) #hyperparameter 2
alpha = 2                #ZI parameter
q = p^alpha              #prob presence

beta_1=delta*p            #beta-bin parameter 1
beta_2=delta*(1-p)        #beta-bin parameter 2
rb = rbeta(nx, beta_1, beta_2, ncp = 0)

y = rep(0,nx)            #generating data
abs.pres = rbinom(nx,1,q)
y[abs.pres==1] = rbinom( sum(abs.pres>0), n.trial, rb[abs.pres==1])

formula = y ~ x +1

```

```

r = inla(formula, data = data.frame(x,y), family = "zeroinflatedbetabinomial2",
        control.family = list(hyper=list(a = list(prior = "flat", param=numeric(0)),
                                                b = list(prior = "flat", param=numeric(0)))),
        Ntrials = rep(n.trial, nx),
        verbose=TRUE)

```